

Warm Up 1

Determine if the set is finite or infinite:

1. {Even numbers greater than 4, but less than 100} *finite*
2. {odd numbers} *infinite*
3. {Fractions less than 1} *infinite*
4. -3 is a member of what set(s)? *integers, rational & real*
5. $\sqrt{2}$ is a member of what set(s)? *irrational (real)*

Cast of Characters

Set-Builder Notation

Naturals

$1, 2, 3, \dots$

Wholes

$0, 1, 2, 3, \dots$

Integers

$\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

Rationals

$0.\bar{3}, \frac{1}{2}, \dots$

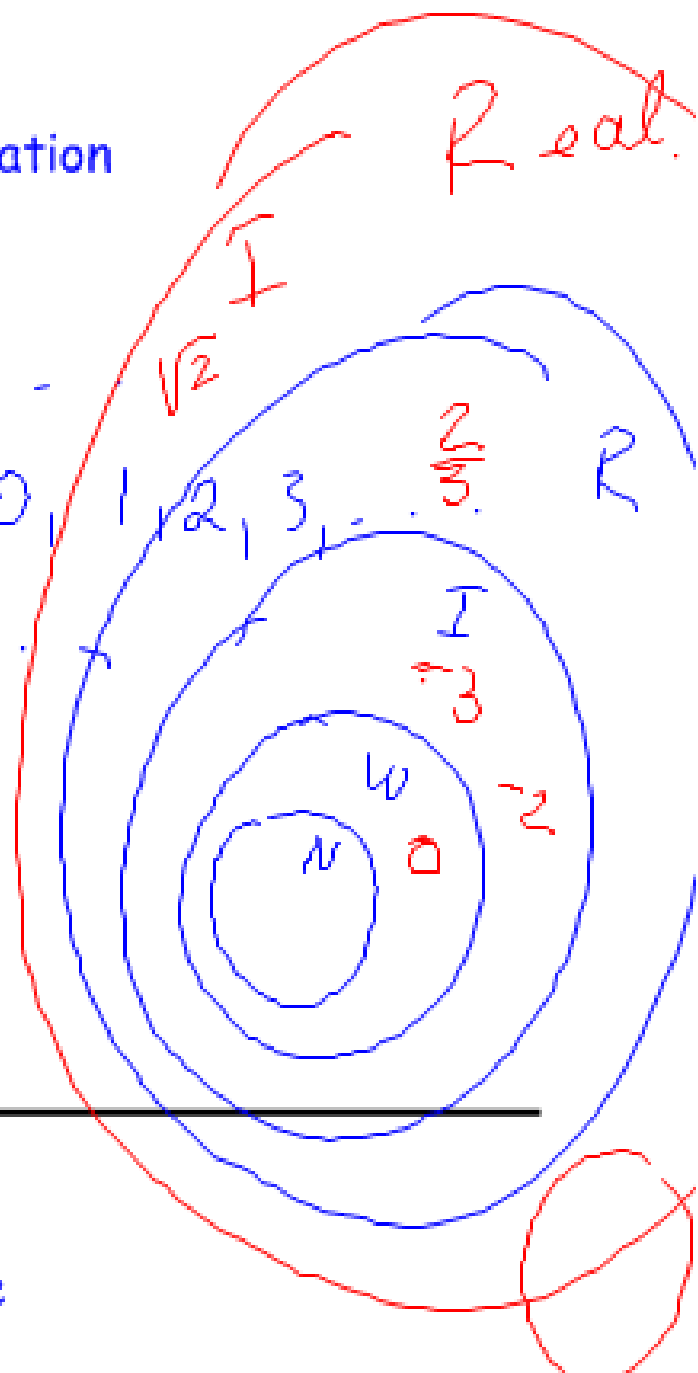
Irrationals

$\sqrt{5}, \sqrt{2}, \dots$

Reals

$0.33345\dots$

$0.\bar{3}$



Real Number Line



Rational Numbers

Repeating

$$\frac{1}{3} = 0.333\dots = 0.\overline{3}$$

Terminating

$$\frac{1}{2} = 0.5$$

Set-Builder Notation

$\{a/b \mid a, b \text{ are Integers, } b \neq 0\}$

$$\frac{\cancel{2.3}}{5} \quad \frac{\cancel{5}}{0}$$

Irrational Numbers

$$\sqrt{5} ; 3\sqrt{7} ; \pi$$

$-\infty$

Order and Interval Notation

Inequality Symbols

Unbounded Interval

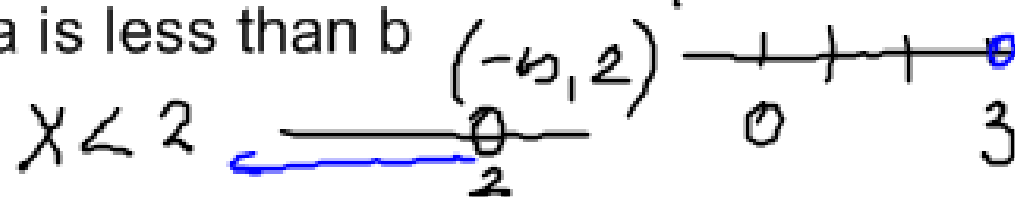
a is greater than b

$$x > 3 \quad (3, +\infty)$$

Interval Notation

$$a > b$$

a is less than b



$$a < b$$

a is greater than or equal to b



$$a \geq b$$

a is less than or equal to b

$$x \leq -4 \quad (-\infty, -4]$$

$$a \leq b$$

Trichotomy Property

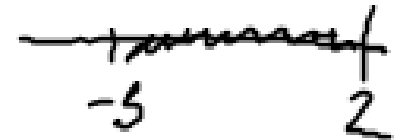
Let a and b be any two real numbers.
Exactly one of the following is true:

$$a > b \quad \text{OR} \quad a = b \quad \text{OR} \quad a < b$$

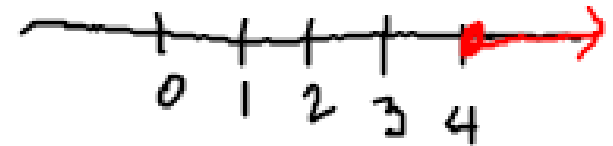
Intervals $()$; $[]$; $]$; $[$

The real numbers between -3 and 2

$$(-3, 2)$$



The real numbers greater than or equal to 4



Bounded Intervals of Real Numbers

let a and b be real numbers with $a < b$

$$[4, \infty)$$

Interval Notation	Interval Type	Inequality Notation	Graph
$[a, b]$	Closed		
(a, b)	Open		
$[a, b)$	Half-Open		
$(a, b]$	Half-Open		

a b



Study table of Unbounded Interval types

Basic Properties of Algebra

Commutative	Addition $u+v=v+u$	Multiplication $uv=vu$
Associative	$(u+v)+w=u+(v+w)$	$(uv)w=u(vw)$
Identity	$u+0=u$	$u \cdot 1=u$
Inverse	$u+(-u)=0$	$u \cdot (1/u)=1, u \neq 0$
Distributive	$(u+v)w=uw+vw$ $u(v+w)=uv+uw$	

$(u-v)w=uw-vw$
 $u(v-w)=uv-uw$

$2 + (3 \cdot 5) \neq (2+3) \cdot (2+5)$
 Does not exist

Additive Inverse Properties

$$-(-u)=u$$

$$-(-2) = 2$$

$$(-u)v = u(-v) = -(uv)$$

$$(-1)3 = 1(-3) = -(1 \cdot 3)$$

$$(-u)(-v) = uv$$

$$(-4)(-3) = 4 \cdot 3$$

$$(-1)u = -u$$

$$(-1) \cdot 5 = -5$$

$$-(u+v) = (-u) + (-v)$$

$$-(2+3) = -2 + (-3)$$

Integer Exponents

Exponential Notation

If a is a real number, variable, or algebraic expression and n is a positive integer, then

$$a^n = \underbrace{a \cdot a \cdot a \cdot a \cdots a}_{n \text{ times}}$$

with n factors of a

exponent n

base a

nth power of a a^n

Properties of Exponents

$$u^m u^n = u^{m+n}$$

$$2^6 \cdot 2^7 = 2^{6+7} = 2^{13}$$

$$(u^m)/(u^n) = u^{m-n}$$

$$\frac{9^3}{9^2} = 9^{3-2} = 9^1 = 9$$

$$u^0 = 1$$

$$8^0 = 1$$

$$u^{-n} = 1/(u^n)$$

$$5^{-3} = \frac{1}{5^3}$$

$$(uv)^m = u^m v^m$$

$$(4 \cdot 5)^{20} = 4^{20} \cdot 5^{20}$$

$$(u^m)^n = u^{mn}$$

$$(7^2)^3 = 7^{2 \cdot 3} = 7^6$$

$$(u/v)^m = (u^m)/(v^m)$$

$$\left(\frac{2}{1}\right)^2 = \frac{2^2}{1^2}$$

Scientific Notation

Used for really large or really small numbers.

Represents a number as a product of:
a number between 1 and 10
times
a power of ten

Convert to and from scientific notation

$$97354100034 = 9.7354100034 \times 10^{10}$$
$$0.0000354717 = 3.54717 \times 10^{-5}$$

P.1 Assignment

Pages 11-13

Edmodo:#2,18,20,30,32,40,42,44,
54,58,60

Paper-based:#5,7,9,13,18,25,27,33,
37,47,51, 53,57,63