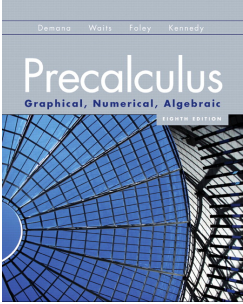


P.5

Solving Equations Graphically, Numerically and Algebraically



PEARSON
Addison Wesley
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What you'll learn about

- Solving Equations Graphically
- Solving Quadratic Equations
- Approximating Solutions of Equations Graphically
- Approximating Solutions of Equations Numerically with Tables
- Solving Equations by Finding Intersections

... and why

These basic techniques are involved in using a graphing utility to solve equations in this textbook.

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Example Solving by Finding x -Intercepts

Solve the equation $2x^2 - 3x - 2 = 0$ graphically.

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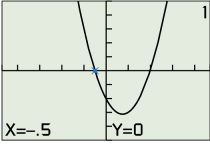
Solution

Solve the equation $2x^2 - 3x - 2 = 0$ graphically.

Find the x -intercepts of $y = 2x^2 - 3x - 2$.

Use the Trace to see that $(-0.5, 0)$ and $(2, 0)$ are x -intercepts.

Thus the solutions are $x = -0.5$ and $x = 2$.



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Zero Factor Property

Let a and b be real numbers.
If $ab = 0$, then $a = 0$ or $b = 0$.

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Quadratic Equation in x

A **quadratic equation in x** is one that can be written in the form

$$ax^2 + bx + c = 0,$$

where a , b , and c are real numbers with $a \neq 0$.

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Completing the Square

To solve $x^2 + bx = c$ by **completing the square**, add $(b/2)^2$ to both sides of the equation and factor the left side of the new equation.

$$x^2 + bx + \left(\frac{b}{2}\right)^2 = c + \left(\frac{b}{2}\right)^2$$
$$\left(x + \frac{b}{2}\right)^2 = c + \frac{b^2}{4}$$

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Quadratic Formula

The solutions of the quadratic equation $ax^2 + bx + c = 0$, where $a \neq 0$, are given by the **quadratic formula**

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

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Example Solving Using the Quadratic Formula

Solve the equation $2x^2 + 3x - 5 = 0$.

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Solution

Solve the equation $2x^2 + 3x - 5 = 0$.

$$a = 2, b = 3, c = -5$$
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-3 \pm \sqrt{3^2 - 4(2)(-5)}}{2(2)}$$
$$= \frac{-3 \pm \sqrt{49}}{4} = \frac{-3 \pm 7}{4}$$
$$x = -\frac{5}{2} \text{ or } x = 1.$$

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Solving Quadratic Equations Algebraically

These are four basic ways to solve quadratic equations algebraically.

1. Factoring
2. Extracting Square Roots
3. Completing the Square
4. Using the Quadratic Formula

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Agreement about Approximate Solutions

For applications, round to a value that is reasonable for the context of the problem. For all others round to two decimal places unless directed otherwise.

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Example Solving by Finding Intersections

Solve the equation $-2|x - 2| = -3$.

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Solution

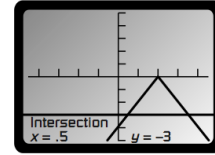
Solve the equation $-2|x - 2| = -3$.

Graph $y = -2|x - 2|$ and $y = -3$.

Use Trace or the intersect feature of your grapher to find the points of intersection.

The graph indicates that the solutions are

$x = 0.5$ and $x = 3.5$.



$[-4.7, 4.7]$ by $[-5, 5]$

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Quick Review

Expand the product.

1. $(x + 2y)^2$
2. $(2x + 1)(4x - 3)$

Factor completely.

3. $x^3 + 2x^2 - x - 2$
4. $y^4 + 5y^2 - 36$
5. Combine the fractions and reduce the resulting fraction

to lowest terms. $\frac{x}{2x+1} - \frac{2}{x-1}$

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Quick Review Solutions

Expand the product.

1. $(x + 2y)^2 = x^2 + 4xy + 4y^2$
2. $(2x + 1)(4x - 3) = 8x^2 - 2x - 3$

Factor completely.

3. $x^3 + 2x^2 - x - 2 = (x + 1)(x - 1)(x + 2)$
4. $y^4 + 5y^2 - 36 = (y^2 + 9)(y - 2)(y + 2)$

5. Combine the fractions and reduce the resulting fraction

to lowest terms. $\frac{x}{2x+1} - \frac{2}{x-1} = \frac{x^2 - 5x + 2}{(2x+1)(x-1)}$

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