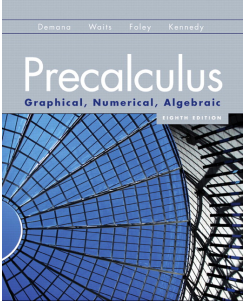


P.4

Lines in the Plane



PEARSON
Addison
Wesley

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What you'll learn about

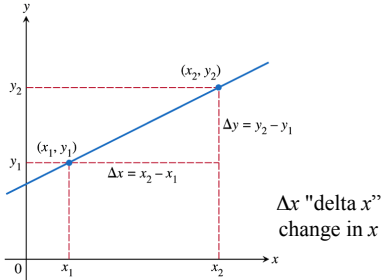
- Slope of a Line
- Point-Slope Form Equation of a Line
- Slope-Intercept Form Equation of a Line
- Graphing Linear Equations in Two Variables
- Parallel and Perpendicular Lines
- Applying Linear Equations in Two Variables

... and why

Linear equations are used extensively in applications involving business and behavioral science.

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Slope of a Line



Δy "delta y"
change in y

Δx "delta x"
change in x

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Slope of a Line

The slope of the nonvertical line through the points (x_1, y_1) and (x_2, y_2) is $m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$.

If the line is vertical, then $x_1 = x_2$ and the slope is undefined.

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Example Finding the Slope of a Line

Find the slope of the line containing the points $(3, -2)$ and $(0, 1)$.

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Example Finding the Slope of a Line

Find the slope of the line containing the points $(3, -2)$ and $(0, 1)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - (-2)}{0 - 3} = \frac{3}{-3} = -1$$

Thus, the slope of the line is -1 .

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Point-Slope Form of an Equation of a Line

The **point - slope form** of an equation of a line that passes through the point (x_1, y_1) and has slope m is $y - y_1 = m(x - x_1)$.

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Slope-Intercept Form of an Equation of a Line

The **slope-intercept form** of an equation of a line with slope m and y-intercept $(0, b)$ is $y = mx + b$.

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Forms of Equations of Lines

General form: $Ax + By + C = 0$,
 A and B not both zero

Slope-intercept form: $y = mx + b$

Point-slope form: $y - y_1 = m(x - x_1)$

Vertical line: $x = a$

Horizontal line: $y = b$

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Graphing with a Graphing Utility

To draw a graph of an equation using a grapher:

1. Rewrite the equation in the form $y =$ (an expression in x).
2. Enter the equation into the grapher.
3. Select an appropriate viewing window.
4. Press the “graph” key.

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Viewing Window

```

WINDOW
Xmin=-10
Xmax=10
Xscl=1
Ymin=-10
Ymax=10
Yscl=1
Xres=1
    
```

[-4, 6] by [-3, 5]

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Parallel and Perpendicular Lines

1. Two nonvertical lines are parallel if and only if their slopes are equal.
2. Two nonvertical lines are perpendicular if and only if their slopes m_1 and m_2 are opposite reciprocals.

That is, if and only if $m_1 = -\frac{1}{m_2}$.

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Example Finding an Equation of a Parallel Line

Find an equation of a line through $(2, -3)$ that is parallel to $4x + 5y = 10$.

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Solution

Find an equation of a line through $(2, -3)$ that is parallel to $4x + 5y = 10$.

Find the slope of $4x + 5y = 10$.

$$5y = -4x + 10$$

$$y = -\frac{4}{5}x + 2 \quad \text{The slope of this line is } -\frac{4}{5}.$$

Use point-slope form:

$$y + 3 = -\frac{4}{5}(x - 2) \quad \text{so } y = -\frac{4}{5}x - \frac{7}{5}$$

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Example Finding an Equation of a Perpendicular Line

Find an equation of a line through $P(-4, 5)$ that is perpendicular to the line L with equation $2x - y = 1$.

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Solution

Find an equation of a line through $P(-4, 5)$ that is perpendicular to the line L with equation $2x - y = 1$.

Find the slope of $2x - y = 1$.

$$-y = -2x + 1$$

$$y = 2x - 1 \quad \text{Slope is } 2.$$

Perpendicular slope is $-\frac{1}{2}$. Use point-slope form:

$$y - 5 = -\frac{1}{2}(x - (-2)) \quad \text{so } y = -\frac{1}{2}x + 3$$

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Example Finding a Linear Model

American's disposable income in trillions of dollars is given in the table on the next slide.

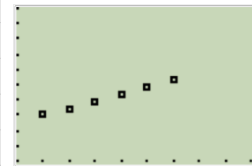
- Write a linear equation for Americans' disposable income y in terms of the year x using the points $(2002, 8)$ and $(2004, 8.9)$.
- Use the equation in (a) to estimate Americans' disposable income in 2005.
- Use the equation in (a) to predict Americans' disposable income in 2010.
- Superimpose a graph of the linear equation in (a) on a scatter plot of the data.

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Example Finding a Linear Model

Year	Amount (trillions of dollars)
2002	8
2003	8.4
2004	8.9
2005	9.3
2006	9.9
2007	10.4



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Solution

(a) Let $y = mx + b$. Find the slope $m = \frac{8.9 - 8}{2004 - 2002} = 0.45$

Use (2002, 8) to find b .

$$y = 0.45x + b$$

$$8 = 0.45(2002) + b$$

$$b = 8 - 900.9 = -892.9$$

$$y = 0.45x - 892.9$$

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Solution

(b) Find y when $x = 2005$.

$$y = 0.45x - 892.9$$

$$y = 0.45(2005) - 892.9$$

$$y = 9.35$$

So we estimate Americans' disposable income in 2005 to be 9.35 trillion dollars, a little more than the actual amount of 9.3 trillion dollars.

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Solution

(c) Find y when $x = 2010$.

$$y = 0.45x - 892.9$$

$$y = 0.45(2010) - 892.9$$

$$y = 11.6$$

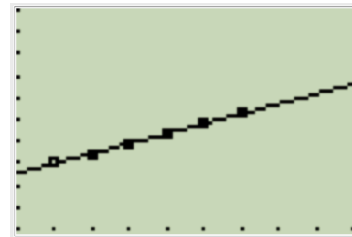
So we predict Americans' disposable income in 2010 to be 11.6 trillion dollars.

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Solution

(d) Here's the graph and scatter plot.



[2001,2010] by [5, 15]

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Quick Review

Solve for x .

1. $-50x + 100 = 200$

2. $3(1 - 2x) + 4(x + 2) = 10$

Solve for y .

3. $2x - 3y = 5$

4. $2x - 3(x + y) = y$

5. Simplify the fraction. $\frac{7 - 2}{-10 - (-3)}$

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Quick Review Solutions

Solve for x .

1. $-50x + 100 = 200$ $x = -2$

2. $3(1 - 2x) + 4(x + 2) = 10$ $x = \frac{1}{2}$

Solve for y .

3. $2x - 3y = 5$ $y = \frac{2x - 5}{3}$

4. $2x - 3(x + y) = y$ $y = \frac{-x}{4}$

5. Simplify the fraction. $\frac{7 - 2}{-10 - (-3)} = \frac{-5}{7}$

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