

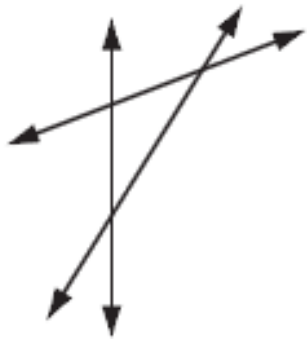
3.7 & 3.8 Constructing Points of Concurrency and Centroid

Objectives:

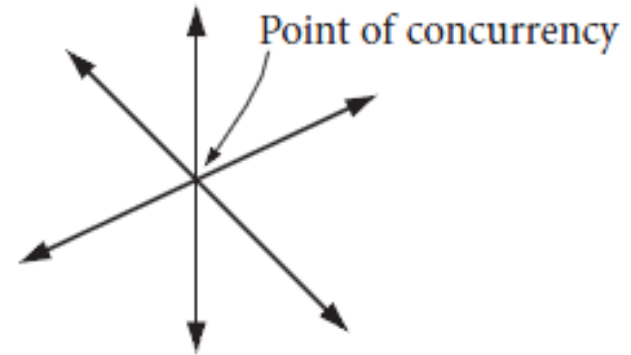
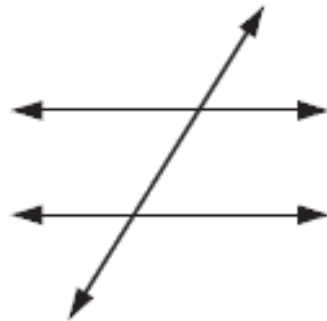
- I CAN discover points of concurrency of the angle bisectors, perpendicular bisectors, and altitudes of a triangle.
- I CAN explore the relationships between points of concurrency and inscribed and circumscribed circles.
- I CAN discover the concurrence of the medians of a triangle (the centroid) and its applications.
- I CAN explore length relationships among the segments into which the centroid divides each median.

Points of Concurrency

- What does Concurrent mean?



Not concurrent



Concurrent

Points of Concurrency

Point of concurrency: The place where three or more lines meet.

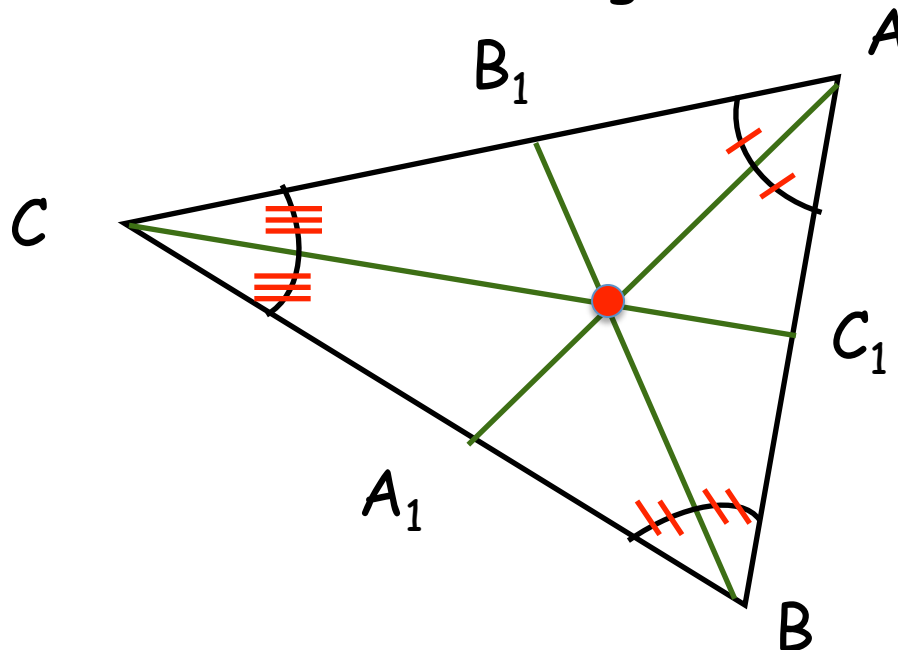
Make a checklist:

- | | | |
|--------------------------|--------------|---------------------------|
| <input type="checkbox"/> | Incenter | (angle bisectors) |
| <input type="checkbox"/> | Circumcenter | (perpendicular bisectors) |
| <input type="checkbox"/> | Orthocenter | (altitudes) |
| <input type="checkbox"/> | Centroid | (medians) |

Points of Concurrency

Incenter (angle bisectors)

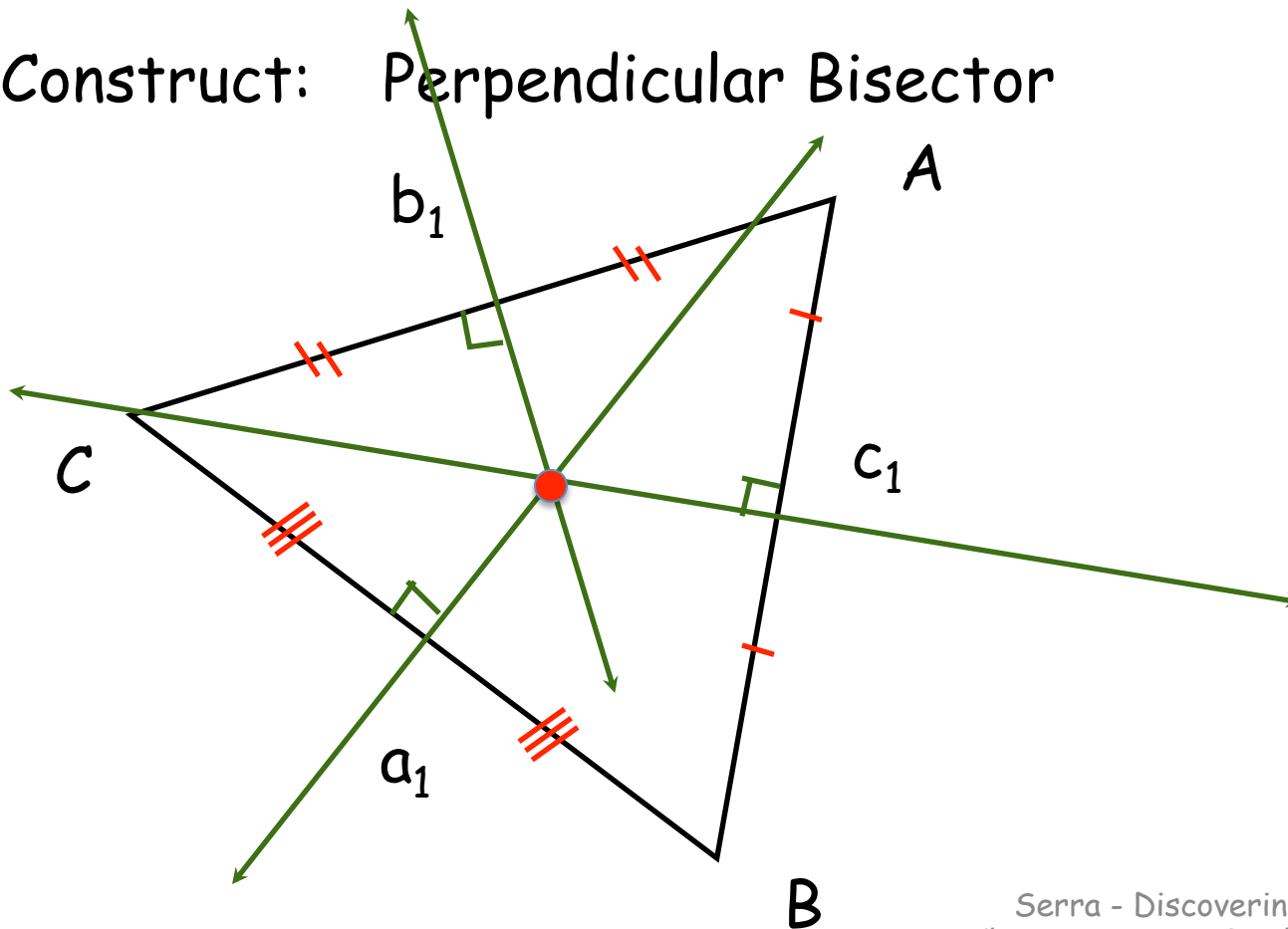
Construct: Angle Bisector



Points of Concurrency

Circumcenter (perpendicular bisectors)

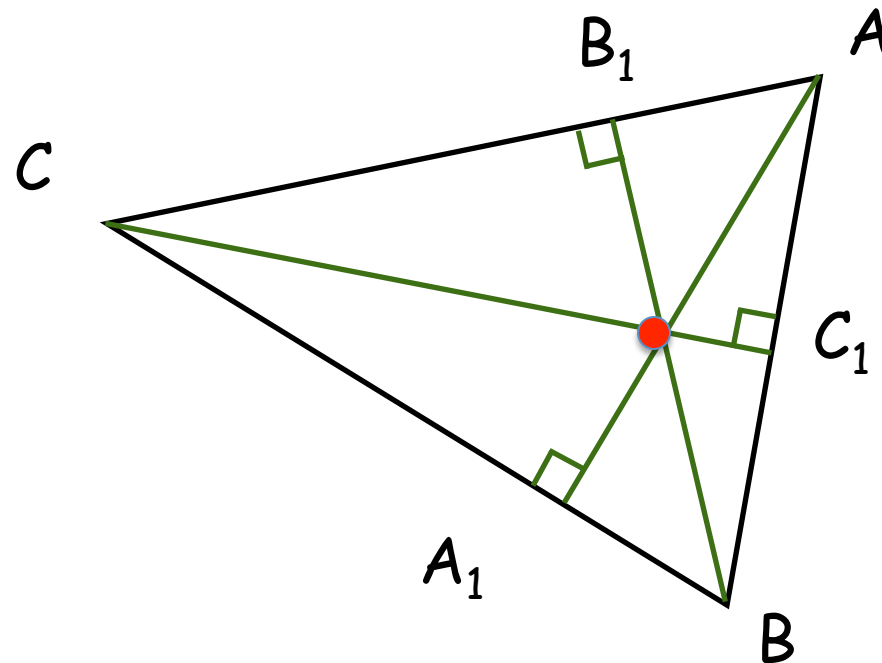
Construct: Perpendicular Bisector



Points of Concurrency

Orthocenter (altitudes)

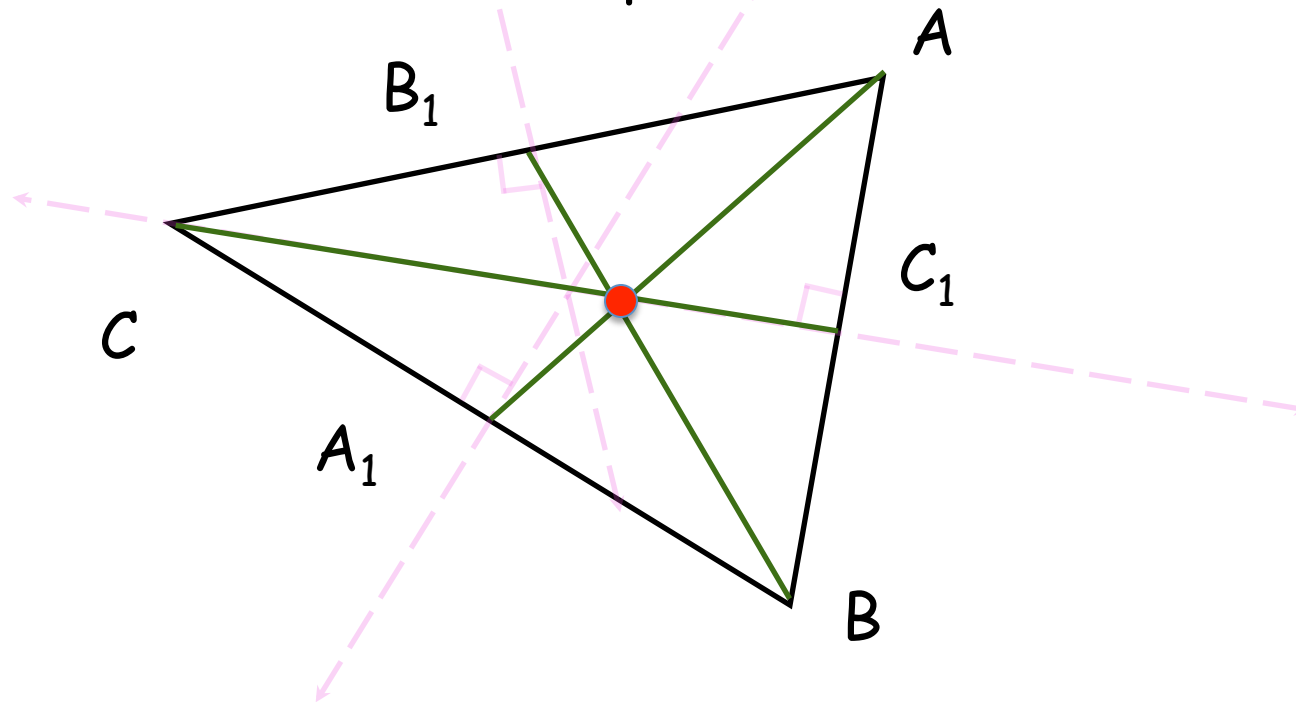
Construct: Drop a perpendicular.



Points of Concurrency

Centroid (median)

Construct: Perpendicular Bisectors



Conjectures

Angle Bisector Concurrency Conjecture

The three angle bisectors of a triangle meet at a point (are concurrent).

Perpendicular Bisector Concurrency Conjecture

The three perpendicular bisectors of a triangle are concurrent.

Altitude Concurrency Conjecture

The three altitudes (or lines containing the altitudes) of a triangle are concurrent.

More Conjectures

Circumcenter Conjecture

The circumcenter of a triangle is equidistant from the vertices.

Incenter Conjecture

The incenter of a triangle is equidistant from the sides.

Median Concurrency Conjecture

The three medians of a triangle are concurrent.

Two More Conjectures

Centroid Conjecture

The centroid of a triangle divides each median into two parts so that the distance from the centroid to the vertex is twice the distance from the centroid to the midpoint of the opposite side.

Center of Gravity Conjecture

The centroid of a triangle is the center of gravity of the triangular region.

Construction 17-20: Lines in a Triangle

| Type | Intersection of: | Special Characteristics |
|--------------------------------------|---------------------------------|--|
| <u>Con 8:</u> <u>Incenter</u> | Angle Bisectors | Same distance from sides. Center of the circle inscribed in the triangle. |
| <u>Con 9:</u> <u>Circumcenter</u> | Perpendicular Bisectors (Sides) | Same distance from vertices. Center of the circle circumscribed about the triangle. |
| <u>Con 10:</u> <u>Orthocenter</u> | Altitudes (heights) | |
| <u>Con 11:</u> <u>Centroid</u> | Medians | $\frac{2}{3}$ distance from vertex to midpoint of opposite side. |

Vocabulary

E Concurrent

A) The point of concurrency for the three angle bisectors is the incenter.

D Point of
Concurrency

B) The point of concurrency for the three altitudes.

A
Incenter

C) The point of concurrency for the perpendicular bisector.

C
Circumcenter

B
Orthocenter

D) The point of intersection

E) Three or more line have a point in common.

Vocabulary

C Circumscribed

A) To draw (one figure) within another figure so that every vertex of the enclosed figure touches the outer figure.

A Inscribed

B) The balancing point for a polygon.

D Centroid

C) To enclose a polygon within a configuration of lines, curves, or surfaces so that every vertex of the enclosed object is lying on the enclosing configuration.

B Center of Gravity

D) The point of concurrency of the three medians.

Project

Choose the project that you will do with your partner.

The projects will be presented on: